

Name: Solutions

Math 130

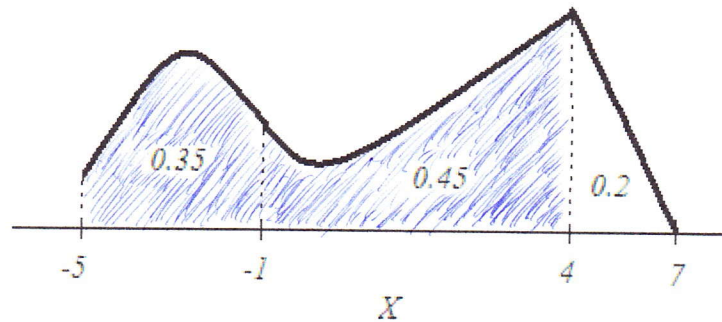
Date: 3/12/2025

Quiz 9

1. (2 points) State the requirements for a density curve (for a continuous random variable).

- ① The curve must be on or above the x-axis
- ② The area under the entire curve must equal 1.

2. (3 points) Suppose  $X$  is a random variable with the density curve drawn below.



a) What are the possible values of  $X$ ?

All decimals between -5 and 7.

b) What is  $P(X = 4)$ ?

$\boxed{0}$

c) What is  $P(-7 \leq X \leq 4)$ ?

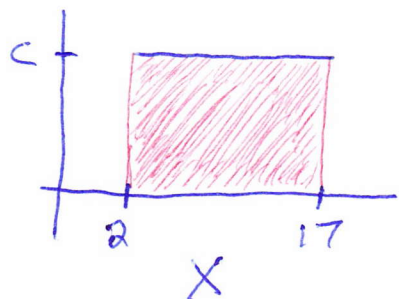
$$= P(-5 \leq x \leq 4)$$

$$= 0.35 + 0.45$$

$$= \boxed{0.8}$$

3. (2 points) Suppose  $X$  is uniformly distributed over the interval  $[2, 17]$ .

a) Find  $c$  that makes this a probability density.



Area under  
entire curve = 1

$$b \cdot h = 1$$

$$15c = 1$$

$$\frac{15c}{15} = \frac{1}{15}$$

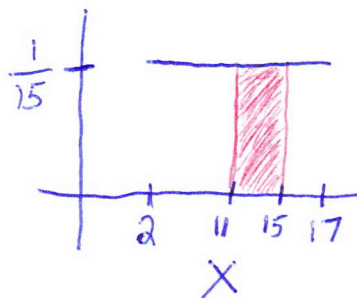
$$\Rightarrow \boxed{c = \frac{1}{15}}$$

b) Find  $P(11 \leq X \leq 15)$

$$= b \cdot h$$

$$= 4 \cdot \frac{1}{15}$$

$$= \boxed{\frac{4}{15}}$$



4. (3 points) Suppose  $Z$  has a standard normal distribution.

a) What are the possible values for  $Z$ ?

All decimals

b) What is the mean  $\mu$  of  $Z$ ?

$$\mu = 0$$

c) What is the standard deviation  $\sigma$  of  $Z$ ?

$$\sigma = 1$$